Introduction to Light Field Analysis

Bastian Goldlücke

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## What do these images tell you about the scene?





## The light field: densely sampled view points





## What if each of these views is actually a light field?









A 2D horizontal cut (green) is called an epipolar plane image (EPI)

## Depth estimation on an epipolar plane image (EPI)





Epipolar plane image (EPI)

## Depth estimation on an epipolar plane image (EPI)





Orientation estimate (structure tensor)

## Depth estimation on an epipolar plane image (EPI)





Orientation estimate (structure tensor)



Depth estimate (slope of orientation)

## Dense depth via orientation estimation





light field center view

estimated depth map (denoised)

[Wanner and Goldluecke CVPR 2012, CVPR 2013, VMV 2013, TPAMI 2014]

## When does depth reconstruction fail?

## Unsolved: "non-cooperative" surfaces



## Stereo image pair





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## Triangulation from correspondence





# Stereo image pair Triangulation from correspondence

**Incorrect assumption:** A 3D point looks the same in all views

## Unsolved: "non-cooperative" surfaces



## Stereo image pair



#### Stereo reconstruction



#### Incorrect assumption: A 3D point looks the same in all views





#### stereo reconstruction



#### epipolar plane image closeup





#### light field

#### stereo reconstruction





#### epipolar plane image closeup

Second order structure tensor:

$$\mathcal{M} = G_{\tau} * \begin{bmatrix} I_{xx}^2 & I_{xx}I_{xy} & I_{xx}I_{yy} \\ I_{xy}I_{xx} & I_{xy}^2 & I_{xy}I_{yy} \\ I_{yy}I_{xx} & I_{yy}I_{xy} & I_{yy}^2 \end{bmatrix},$$

and  $e_1(\mathcal{M})$  encodes the two dominant overlaid orientations.





#### stereo reconstruction



#### epipolar plane image closeup

#### mirror plane depth







#### stereo reconstruction



#### epipolar plane image closeup



#### reflection depth



## Works great on carefully recorded data ...





light field center view



stereo reconstruction



primary surface depth



transmission depth

## Sadly, not good enough for plenoptic cameras





fails due to noise, too large disparity range ...

## More robust layered depth reconstruction

## Robust layered depth from sparse light field coding



. . . .

## Idea: represent each EPI patch with atoms of fixed disparity,



# Robust layered depth from sparse light field coding



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Each light field patch p is assembled from a trained patch dictionary D



by solving the sparse coding problem

$$\operatorname*{argmin}_{\alpha}\left\|\boldsymbol{p}-\boldsymbol{D}\boldsymbol{\alpha}\right\|_{2}^{2}+\lambda\left\|\boldsymbol{\alpha}\right\|_{1}.$$

# Robust layered depth from sparse light field coding



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The coding coefficients  $\alpha$  should be related to the depth layers.

## Interpretation of the sparse codes





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## Classes of aggregated sparse codes





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## Light field decomposition



## Generative model: generates EPI from center view





Depth-dependent linear relation between center view and EPI:

 $f = G(d_u) u,$ 

where

- $d_u$  center view depth (at gray pixels),
- $G(d_u)$  depth-dependent linear transformation,
  - f generated complete EPI.



Two-layer EPI synthesis model





Two-layer EPI synthesis model



## Leads to data fitting cost function

$$D_{EPI}(u, v) = \|G_{d_u}u + G_{d_v}v - f\|_2^2$$

for each individual EPI.



**Dataterm:** sum over all horizontal and vertical EPIs

$$D(u, v) = \sum_{x=1}^{W} D_x(u_x, v_x) + \sum_{y=1}^{H} D_y(u_y, v_y).$$



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$$J(u, v) = \mathsf{T}\mathsf{G}\mathsf{V}_2(u) + \mathsf{T}\mathsf{G}\mathsf{V}_2(v).$$

Total energy:

$$E(u,v) = D(u,v) + \lambda J(u,v)$$

minimize e.g. with primal-dual method [Chambolle and Pock 2010]. [Johannsen, Sulc, Goldluecke VMV 2015]



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# Outlook: intrinsic light field decomposition





Input light field (center view)



Specular component





Albedo

Shading

[Alperovich and Goldluecke, ACCV 2016]

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### Light field camera alignment



[Johannsen, Sulc, Goldluecke ICCV 2015]



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- How to estimate pose for light field cameras?
- How to easily align light fields for panoramas?
  - sparse correspondence only
  - tailored to light field geometry
  - linear algorithm

 Input: light field from pre-calibrated plenoptic camera (i.e. raw image decoded into two-plane parametrization).

# Lytro camera and microlens images







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# Light field geometry





### What is the projection of a 3D point $\boldsymbol{X}$ into a light field?

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A 2D subspace in the 4D ray space, which can be parametrized in 5D homogenous light field coordinates as follows:

$$\underbrace{\begin{bmatrix} 1 & 0 & \frac{f}{Z} & 0 & -\frac{fX}{Z} \\ 0 & 1 & 0 & \frac{f}{Z} & -\frac{fY}{Z} \end{bmatrix}}_{=:M(\mathbf{X},f)} \begin{bmatrix} u \\ v \\ s \\ t \\ 1 \end{bmatrix} = 0.$$

Note: these are just the projection equations of a pinhole camera located in (s, t).

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- In practice, matched features between subaperture images:

$$\{I_i\}_{i=1,\ldots,n} \leftrightarrow \{I'_j\}_{j=1,\ldots,m}.$$

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 obtained e.g. from matching SIFT features across all subaperture images, absurd matches pre-eliminated (if e.g. disparity outside a sensible range).



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• Turns out this is both boring as well as bad.



#### Blackboard time: Plücker ray coordinates and GEC



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Generalized epipolar constraint:

$$\boldsymbol{q}'^{T} \boldsymbol{E} \boldsymbol{q} + \boldsymbol{q}'^{T} \boldsymbol{R} \boldsymbol{m} + \boldsymbol{m}'^{T} \boldsymbol{R} \boldsymbol{q} = 0.$$

where  $E = [t]_{\times} R$  is the essential matrix, and the camera coordinate systems are related by a rotation R and translation t according to

$$\boldsymbol{X}'=R\boldsymbol{X}+t.$$

• Note number of equations:  $n \cdot m$  per correspondence.

#### Linear correspondence constraints in light fields?

**Observation I:** projection from Plücker ray coordinates into homogenous light field coordinates is projective-linear:

$$q'_{3} \begin{bmatrix} u' \\ v' \\ s' \\ t' \\ 1 \end{bmatrix} = \begin{bmatrix} f & 0 & 0 & 0 & 0 & 0 \\ 0 & f & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} R & 0 \\ E & R \end{bmatrix} \begin{bmatrix} q \\ m \end{bmatrix}.$$

**Observation II:** Each ray in a correspondence must lie in the subspace of the correspondence when transformed into the respective other light field.





Given a correspondence

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estimate subspace matrices M and M' for LHS and RHS.



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Abbreviate with  $M_1$  the first three and with  $M_2$  the second three columns of the 2 × 6 matrix M'P(f),

$$M_1R\boldsymbol{q} + M_2R\boldsymbol{m} + M_1E\boldsymbol{q} = 0.$$

Same form as GEC, same algorithm to compute solution. Note: only 2(n + m) equations per correspondence instead of  $n \cdot m$ .



Can be re-arranged to

$$A_E \operatorname{vec}(E) + A_R \operatorname{vec}(R) = 0.$$

with matrices E, R stacked to columns vec(E), vec(R).



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Solution for vec(R) s.t. ||vec(R)|| = 1 satisfies

$$(A_E A_E^+ - I)A_R \operatorname{vec}(R) = \mathbf{0}.$$

Solve using SVD, project to SO(3) to obtain linear estimate for R.



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Linear estimate for t follows from substituting solution for R into above equation.



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Previous work: "iterative refinement", solve for R and t in turn, backproject to allowed space of solutions.

In practice, not necessary if solving for R first instead of E.


Can be done by brute force search, just look for f which minimizes residual in the linear system - not elegant, but works. Full non-linear bundle adjustment as a second step of course possible as well.



	Correspondences	10 matches, 10 projections per point					20 matches, 10 projections per point					10 matches, 20 projections per point				
	Noise level $\sigma_{\rm UV}$	0.2	0.4	0.6	0.8	1.0	0.2	0.4	0.6	0.8	1.0	0.2	0.4	0.6	0.8	1.0
Angular rot. error [deg]	linear methods															
	3DPC	1.82	5.19	8.93	11.56	16.18	1.33	3.42	6.77	8.38	10.24	1.15	4.35	6.43	9.14	14.12
	R2R-O R2R-I	2.04 0.88	11.17 1.91	15.37 3.51	37.48 4.55	43.32 5.19	0.72 0.40	2.19 0.92	3.48 2.13	3.76 2.76	6.41 4.01	1.87 0.55	3.01 1.40	17.56 2.64	39.66 4.20	40.02 5.98
	Proposed	0.65	1.19	1.80	2.28	3.15	0.27	0.52	0.83	1.11	1.49	0.40	0.81	1.27	1.77	2.39
	with refinement															
	R2R-O-R20	1.00	2.05	3.71	4.53	18.40	0.43	0.90	2.31	2.94	4.10	0.62	1.45	9.27	7.86	9.33
	Proposed-R20	0.69	1.20	1.77	2.23	2.85	0.26	0.50	0.79	1.05	1.42	0.37	0.80	1.18	1.57	2.39
Relative transl. error [%]	linear methods															
	3DPC	0.28	0.82	0.93	2.19	2.20	0.32	0.97	0.92	1.44	0.95	0.46	0.84	1.21	0.74	0.86
	R2R-O	0.20	1.15	1.06	4.18	2.01	0.05	0.43	0.30	0.36	0.45	1.68	0.27	1.43	0.98	0.79
	Proposed	0.04	0.12	0.25	0.40	0.52	0.02	0.09	0.14	0.25	0.30	0.12	0.01	0.27	0.24	0.33
	with refinement										-					
	R2R-O-R20 R2R-I-R20	0.05 0.04	0.13 0.13	0.24 0.24	0.51 0.51	0.67 0.51	0.02 0.02	0.09 0.09	0.15 0.15	0.25 0.25	0.36 0.36	0.12 0.12	0.11 0.11	0.41 0.27	0.27 0.25	0.37 0.33
	Proposed-R20	0.03	0.08	0.14	0.26	0.23	0.01	0.05	0.07	0.11	0.14	0.11	0.06	0.16	0.10	0.13

Accuracy of the different methods both before and after non-linear refinement. Different numbers of correspondences N, projections per correspondence K, and levels of noise  $\sigma_{uv}$  on the (u, v)-coordinates are compared. Error metrics are the angular deviation from the ground truth in degrees for the estimated rotation, as well as the relative translation error measured as a percentage of the length of the ground truth translation vector. Noise standard deviation is given in units of pixels on the subaperture images. In all cases, the most accurate method (highlighted in bold) is the one proposed in this paper.

### Accuracy over number of corresponding rays





The graphs show how the angular error in rotation depends on the number of matches (left) and the number of rays per match (right). Compared are the four linear methods in table ??: 3DPC [?] (red) and R2R-O [?] (cyan), R2R-I with our proposed numerical improvements (blue), and finally the novel proposed method for 4D light fields (green). Top row: small amount of noise ( $\sigma = 0.2$ ), bottom: large amount of noise ( $\sigma = 1.0$ ).

# Living panoramas





# Living panoramas





# 3D point cloud







 Simple linear method to estimate pose for light fields in the two-plane parametrization.

More accurate than all previous methods, reduced number of equations compared to framework of generalized cameras.

 Allows simple construction of refocusable light field panoramas, but there's work left to do for high quality.

### Putting it all together - full scene reconstruction

## Let's go back to our challenge dataset





## Light field alignment and bundle adjustment









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### Two-layered depth map estimation







Center view 14  $\,/$  24

Depth second layer









Input

## Summary

#### Sparse light field coding for multi-layer depth [Johannsen, Sulc, Goldluecke CVPR 2016, GCPR 2016]





Light field decomposition and intrinsic light fields [Johannsen, Sulc, Goldluecke VMV 2015, Alperovich and Goldluecke (submitted to ACCV 2016)]

#### Light field alignment and refocusable panoramas [Johannsen, Sulc, Goldluecke ICCV 2015]







#### Multi-layered 3D scene reconstruction [Johannsen, Sulc, Marniok, Goldluecke (submitted)]